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## PHOTOREFRACTIVE PROPERTIES OF DOUBLE-DOPED HF:CE:LINBO<sub>3</sub> CRYSTALS

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**ABSTRACT:** In this article, the double-doped  $Hf:Ce:LiNbO_3$  crystals were grown by the Czochralski method and its photorefractive properties were systematically studied. Samples were treated with different oxidation/ reduction. The photorefractive properties of  $Hf:Ce:LiNbO_3$  crystals were investigated by the two-beam coupling method. The results shown that the photorefractive properties of  $Hf:Ce:LiNbO_3$  crystals were improved as compared with that of  $Ce:LiNbO_3$  crystals. The oxidation/reduction treatment had great effect on the photorefractive properties and the doping mechanism was also discussed. © 2008 Wiley Periodicals, Inc. Microwave Opt Technol Lett 50: 1693–1695, 2008; Published online in Wiley Inter-Science (www.interscience.wiley.com). DOI 10.1002/mop.23448

**Key words:** *Hf*:*Ce*:*LiNbO*<sub>3</sub> *crystal; photorefractive property; oxidation/ reduction treatment* 

#### 1. INTRODUCTION

Lithium niobate (LiNbO<sub>3</sub>, LN) single crystal has been extensively studied because of its excellent ferroelectric, piezoelectric, and photorefractive properties, which is one of the promising candidates for holographic data storage. The photorefractive properties of the LN can be effectively affected by doping with transition metal and rare earth ions, such as Fe [1], Cu [2], Cr [3], Mn [4], Sc [5], Ce [6], Zn [7], Pr [8], Nd [9]. The photorefractive sensitivity of Ce:LiNbO<sub>3</sub> is one order higher than that of congruent undoped LiNbO<sub>3</sub> [6]. But low optical damage resistance ability and long response time are the two main disadvantages of Ce: LiNbO<sub>3</sub>. Doping with damage-resistance dopants is found to be an effective way to solve the problem [10]. Sc [5], Zn [7], Mg [11], In [12], and Hf [13-15] have been used to increase the optical damage resistance ability of LiNbO<sub>3</sub>. In addition, modest oxida-



Figure 1 Experiment setup of the two-beam coupling method

tion or reduction can change the valance state of the doping ions and affect the photorefractive properties of the crystal.

In this article, Hf was employed to enhance the optical damage resistance ability of Ce:LiNbO<sub>3</sub>. Oxidation/reduction treatments were adopted to change the photorefractive properties. The photorefractive properties of Hf:Ce:LiNbO<sub>3</sub> were discussed in detail.

#### 2. CRYSTAL GROWTH AND SAMPLE PREPARATION

The LiNbO<sub>3</sub> crystals doped with 0.1 wt% CeO<sub>2</sub> and 4 mol% HfO<sub>2</sub> were grown by the Czochralski method along the c-axis from the congruent melt. The Ce:LiNbO<sub>3</sub> were grown for comparison. The raw materials were ultra-pure. After precisely weighed and thoroughly mixed, the materials were calcined at 750°C and then sintered at 1150°C for 4 h, respectively. The composition of the raw materials was shown in Table 1.

The LiNbO<sub>3</sub> crystals were grown with the pulling rate of  $1 \sim 2 \text{ mm/h}$  and rotation rate of  $15 \sim 25 \text{ rpm}$  in air. The temperature gradient above the melt was  $30 \sim 40^{\circ}\text{C/cm}$ . After growth, the crystals were polarized at  $1200^{\circ}\text{C}$  with DC current density of 5 mA/cm<sup>2</sup> for 30 mins. Then the polarized crystals were cut to the size of  $10 \text{ mm} \times 2 \text{ mm} \times 10 \text{ mm}$  (a × b × c). Finally the crystals were polished to optical grade.

The powders of  $Li_2CO_3$  and  $Nb_2O_5$  were chosen as the reducing and oxidizing agents, respectively. The reduction treatment was carried out by burying the samples into  $Li_2CO_3$  powder, heated up to 550°C and hold for 24 h; likewise, the oxidation treatment was burying the samples into  $Nb_2O_5$  powder, then heated up to 1150°C and hold for 12 h.

#### 3. MEASUREMENT OF PHOTOREFRACTIVE PROPERTIES

The photorefractive properties of the crystals (diffraction efficiency, response time, and exponential gain coefficient) were measured by the two-beam coupling method. The experimental setup was shown in Figure 1. Both a signal beam and a pump beam originated from an  $Ar^+$  laser ( $\lambda = 514.5$  nm) irradiated on a sample with polarization direction parallel to the *c*-axis of the sample. The diameters of both the pump beam and the signal beam were adjusted to 1 mm. The intensity ratio between them was

TABLE 1 Composition of the Raw Materials

Crystal No.	1	2	3	4	5	6
$\overline{\text{CeO}_2(\text{wt\%})}$	0.1	0.1	0.1	0.1	0.1	0.1
$HfO_2 (mol\%)$	0	0	0	4	4	4
Crystal size (mm <sup>2</sup> )	$\Phi 30  imes 30$	$\Phi 30 \times 30$	$\Phi 30 \times 30$	$\Phi 30 \times 25$	$\Phi 30 \times 25$	$\Phi 30 \times 25$
Sample size (mm <sup>3</sup> )	$10 \times 2 \times 10$					
Treatment	As grown	Reduction	Oxidation	As grown	Reduction	Oxidation

TABLE 2 The Diffraction Efficiency  $\eta$  and Response Time  $\tau$  of the Crystals

Crystal No.	(%)	
1	58	170
2	53	128
3	60	226
4	42	23
5	39	12
6	48	37

1860. The external crossing angle of the two beams was designed as  $2\theta$ .

Diffraction efficiency  $\eta$  is defined as the ratio of the diffraction light intensity  $I_1'$  to the transmission light intensity  $I_1$ ,

$$\eta = \frac{I_1'}{I_1} \times 100\%$$
 (1)

The response time  $\tau$  is defined as the time interval that is from the time of the incident light begins irradiating on the crystal to the time when the diffraction efficiency reaches  $(1-e^{-1})$  of its maximum.

The exponential gain coefficient is one of the important indicators to evaluate the photorefractive properties of the photorefractive crystal, which corresponds to the energy transition from the pump light to the signal light during the information storage process. The exponential gain coefficient  $\Gamma$  is defined as

$$\Gamma = \frac{1}{\delta} \ln \frac{I'_s I_p}{I_s I'_p} \approx \frac{1}{\delta} \ln \frac{I'_s}{I_s}$$
(2)

where  $I'_{\rm s}$  and  $I'_{\rm p}$  ( $I_{\rm s}$  and  $I_{\rm p}$ ) are the transmitted intensities of signal beam and pumping beam with (without) coupling, respectively, and  $\delta$  is the thickness of the sample. When the intensity of the pump beam is much larger than that of the signal beam, the exponential gain coefficient becomes independent of the pump beam intensity (i.e.  $I_{\rm p} \approx I'_{\rm p}$ ).

#### 4. RESULTS AND DISCUSSIONS

The results were shown in Table 2 and Figure 2. It was obvious that the response time  $\tau$  of Hf:Ce:LiNbO<sub>3</sub> was greatly shortened than that of Ce:LiNbO<sub>3</sub>. After reduction treatment, the diffraction



**Figure 2** Experimental curves of  $\Gamma \sim 2\theta$ . (a) No.5 sample of Hf:Ce: LiNbO<sub>3</sub> with reduction treatment. (b) No.4 sample of Hf:Ce:LiNbO<sub>3</sub>. (a) No.6 sample of Hf:Ce:LiNbO<sub>3</sub> with oxidation treatment

efficiency  $\eta$  of the crystals decreased and the response time  $\tau$  was shortened, but the exponential gain coefficient  $\Gamma$  increased. On the contrary, the diffraction efficiency  $\eta$  and the response time  $\tau$  of the oxidized crystals increased, but the exponential gain coefficient  $\Gamma$  decreased.

The response time  $\tau$  could be expressed as [16]

$$\tau = \frac{\varepsilon \varepsilon_0}{\sigma_{\rm ph} + \sigma_{\rm d}} \tag{3}$$

where  $\varepsilon$  and  $\varepsilon_0$  were the relative dielectric constant and the dielectric constant in vacuum, respectively.  $\varepsilon$  was taken as 32 [16].  $\sigma_{ph}$  and  $\sigma_d$  were photoconductivity and dark conductivity, respectively. In the range of our measurement,  $\sigma_d$  could be negligible because  $\sigma_d \ll \sigma_{ph}$ . According to Li vacancy model [17], there were lots of Nb<sub>Li</sub> (Nb atom on the Li vacancy) in congruent LiNbO<sub>3</sub> crystals which acted as electron trap centers. In Hf:Ce:LiNbO<sub>3</sub>, the Nb<sub>Li</sub> decreased as the Hf doping concentration increased, and it was cleared up as the concentration of Hf achieved 4 mol%. So  $\sigma_{ph}$  increased and the response time of Hf:Ce:LiNbO<sub>3</sub> was greatly shortened.

Further more, oxidation/reduction could affect the concentrations of the electron donor and acceptor. The concentrations of the lower valence Ce<sup>3+</sup> and the oxygen vacancy (Vo +2e) increased after reduction. They gave out electrons when the laser irradiated on the crystal, so the  $\sigma_{ph}$  increased and the photorefractive performance of the crystal was enhanced though the diffraction efficiency was little decreased.

#### 5. CONCLUSION

The photorefractive properties of Hf:Ce:LiNbO<sub>3</sub> were enhanced as compared with that of Ce:LiNbO<sub>3</sub>. The oxidation/reduction treatment had significant effect on the photorefractive properties. The reduced Hf:Ce:LiNbO<sub>3</sub> showed favorable photorefractive properties and was a promising holographic storage media.

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# A NOVEL DUAL-FREQUENCY UNEQUAL WILKINSON POWER DIVIDER

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ABSTRACT: This article presents the design of a novel dual-frequency unequal Wilkinson power divider. This unequal power divider fulfills an arbitrary power split and all the other features of a conventional Wilkinson unequal power divider simultaneously at two arbitrary frequencies. The structure of this power divider and the formulas used to determine the design parameters have been given. Both simulated and measured results of the dual-frequency unequal Wilkinson power divider are presented to validate our proposed idea. Good experimental performances of the proposed power divider, including an arbitrary power split and a good isolation between the output ports at both frequencies are obtained. © 2008 Wiley Periodicals, Inc. Microwave Opt Technol Lett 50: 1695–1699, 2008; Published online in Wiley InterScience (www.interscience.wiley.com). DOI 10.1002/mop.23447

#### 1. INTRODUCTION

The power divider is one of the most popular passive circuits used for microwave and millimeter-wave applications. In a very recent publication [1], a dual-frequency unequal power divider has been presented. A suitable optimization procedure was applied using genetic algorithms in order to satisfy several requirements at both frequencies. This power divider was designed by numerical solution, which, although not analytically exact, was numerically nearly exact. Here, we present a true exact solution to the dualfrequency unequal power divider with a dual-band transformer section, which has been introduced by Monzon in [2]. A dualfrequency equal Wilkinson power divider with this transformer section has been reported in [3], the authors used the even and odd mode analysis to determine the circuit parameters. But for considering the special requirements of the dual-frequency transformer section, and the unique characteristic of the unequal power divider, there is still no exact solution to the dual-frequency unequal power divider. Therefore, we present an extension of Monzon's analysis to the design of a dual-frequency unequal power divider. The proposed power divider operates at two arbitrary frequencies of interest  $f_1$  and  $f_2$ , and at an arbitrary power split. The design parameters of the dual-frequency unequal Wilkinson power divider are presented in explicit closed form. The validity of this analysis is demonstrated by experimental results with a power split of 2:1 and a power split of 1.5:1 at 0.9 GHz and 1.8 GHz, which are applied in present global system for mobile communication (GSM) and personal communication system (PCS), and with a power split of 2:1 at 0.915 GHz and 2.45 GHz, which are applied in RFID.

#### 2. THEORY AND DESIGN EQUATIONS

In a conventional Wilkinson unequal power divider, the output ports are shunted with a parallel connection of a resistor *R*. If the power split at Ports 2 and 3 is  $K^2 = P_3/P_2$ , we can consider that the output ports are matching with the impedance  $R_2 = Z_0 K$  and  $R_3 = Z_0/K$  [4], where  $Z_0$  is the reference impedance. The characteristic impedance of each branch and the resistor *R* are given by [4]:

$$Z_{03} = Z_0 \sqrt{\frac{1+K^2}{K^3}}$$
(1)

$$Z_{02} = K^2 Z_{03} = Z_0 \sqrt{K(1+K^2)}$$
(2)

$$R = Z_0 \left( K + \frac{1}{K} \right) \tag{3}$$

This conventional Wilkinson unequal power divider operates at one design frequency  $f_1$  and at all its odd harmonics. Therefore, it is not suitable for some dual-band operations. In 2003, a small dual-frequency transformer section has been introduced by Monzon in [2], which could operate at any two arbitrary  $f_1$  and  $f_2$ . For using Monzon's Theory in the design of a dual-frequency unequal power divider, each quarter-wave branch of a conventional Wilkinson unequal power divider is substituted by transformer in two sections with the characteristic impedance of  $Z_1$  and  $Z_2$  and the length of L, respectively. A schematic diagram of the proposed Wilkinson unequal power divider, which operates at two arbitrary frequencies and at an arbitrary power split, is shown in Figure 1.

When Monzon's Theory is applied, it is necessary to determine the input and output impedance of each branch in the unequal power divider. In a conventional unequal Wilkinson power divider, each branch is a  $\lambda/4$  transformer section. Assuming that the characteristic impedance of this section is  $Z_0$ , we can obtain  $Z_{in}$  as

$$Z_{\rm in} = Z_0^2 / Z_{\rm out} \tag{4}$$

By using (1) and (2) in (4), with  $Z_{out2} = R_2 = Z_0 K$  and  $Z_{out3} = R_3 = Z_0 / K$ , respectively,  $Z_{ina}$  and  $Z_{inb}$  can be obtained as

$$Z_{ina} = Z_0 (1 + K^2)$$
(5)

$$Z_{inb} = Z_0 \bigg( 1 + \frac{1}{K^2} \bigg) \tag{6}$$